

# LECTURE 10

L10

Fourier transform of  $f(x)$

defined on  $-\infty < x < +\infty$

$$g(k) = \frac{1}{2\pi} \int_{-\infty}^{\infty} f(x) e^{-ikx} dx \quad k = \frac{2\pi}{\lambda}$$

Inverse Fourier transform

$$f(x) = \int_{-\infty}^{\infty} g(k) e^{ikx} dk$$

Plane wave  $e^{i(kx - \omega t)}$

Phase "velocity"

$$v_p = \begin{cases} \frac{\omega}{k} & \text{to R if } x, t \text{ opposite signs} \\ .. L .. .. same .. & \end{cases}$$

Ordinary wave eqn.  $\frac{\partial^2 \phi}{\partial x^2} = \frac{1}{c^2} \frac{\partial^2 \phi}{\partial t^2}$

- plane wave is separable solution if  
 $\omega(k) = ck$

- phase velocity

$$v_p = c \quad \text{independant of } k$$

nondispersive